

**LAMPIRAN A**  
**NOTASI**

## NOTASI

$V$	:	Kecepatan Albatross
$v$	:	kecepatan
$g$	:	Percepatan gravitasi bumi
$D$	:	Gaya gesek
$L$	:	Gaya angkat
$H$	:	Hamiltonian
$h$	:	Ketinggian
$J$	:	Indeks kinerja
$m$	:	Massa Albatross
$S$	:	Luas sayap Albatross
$k$	:	Faktor gaya gesek
$\alpha$	:	Sudut serang
$\chi_a$	:	Sudut belok
$\gamma_a$	:	Sudut tanjak
$\mu_a$	:	Sudut putar
$C_L$	:	Koefisien gaya angkat
$C_D$	:	Koefisien gaya gesek
$u, v, w$ $kg \quad kg \quad kg$	:	Komponen kecepatan
$x, y, z$ $g \quad g \quad g$	:	Koordinat sistem
$V_k$	:	Kecepatan inersia
$V_w$	:	Kecepatan angin
$\lambda$ $i$	:	Lagrange multipliers

**LAMPIRAN B**  
**PENURUNAN RUMUS**

### Penurunan persamaan sudut belok optimal ( $\mu_a$ )<sub>opt</sub> ) tanpa kendala

Berdasarkan persamaan (3.1) dan persamaan (3.2) didapatkan penurunan-penurunan sebagai berikut:

- $$0 = \left( \frac{\sin \mu_a \sin \gamma_a \cos \chi_a - \cos \mu_a \sin \chi_a}{m} \right) \lambda_u + \left( \frac{\sin \mu_a \sin \gamma_a \sin \chi_a + \cos \mu_a \cos \chi_a}{m} \right) \lambda_v$$

$$+ \left( \frac{\sin \mu_a \cos \gamma_a}{m} \right) \lambda_w$$
- $$0 = \sin \mu_a \left[ \frac{\sin \gamma_a \cos \chi_a \lambda_u}{m} + \frac{\sin \gamma_a \sin \chi_a \lambda_v}{m} + \frac{\cos \gamma_a \lambda_w}{m} \right]$$

$$+ \cos \mu_a \left[ \frac{-\sin \chi_a \lambda_u}{m} + \frac{\cos \chi_a \lambda_v}{m} \right]$$
- $$-\sin \mu_a \left[ \frac{\lambda_u \sin \gamma_a \cos \chi_a + \lambda_v \sin \gamma_a \sin \chi_a + \lambda_w \cos \gamma_a}{m} \right] = \cos \mu_a \left[ \frac{-\lambda_u \sin \chi_a + \lambda_v \cos \chi_a}{m} \right]$$

### Penurunan persamaan koefisien gaya angkat optimal (( $C_L$ )<sub>opt</sub> ) tanpa kendala

Berdasarkan persamaan (3.4), persamaan (3.1), persamaan (2.2.3), persamaan (2.2.4), dan persamaan (2.2.5) didapatkan penurunan-penurunan sebagai berikut:

- $$0 = \frac{-\cos \gamma_a \cos \chi_a 2k C_L \left( \frac{\rho}{2} \right) V^2 S \lambda_u}{m} - \left[ \frac{(\cos \mu_a \sin \gamma_a \cos \chi_a + \sin \mu_a \sin \chi_a) \left( \frac{\rho}{2} \right) V^2 S \lambda_u}{m} \right]$$
- $$- \frac{\cos \gamma_a \sin \chi_a 2k C_L \left( \frac{\rho}{2} \right) V^2 S \lambda_v}{m} - \left[ \frac{(\cos \mu_a \sin \gamma_a \sin \chi_a - \sin \mu_a \cos \chi_a) \left( \frac{\rho}{2} \right) V^2 S \lambda_v}{m} \right]$$

$$- \left( \frac{-\sin \gamma_a 2k C_L \left( \frac{\rho}{2} \right) V^2 S \lambda_w}{m} \right) - \frac{\cos \mu_a \cos \gamma_a \left( \frac{\rho}{2} \right) V^2 S \lambda_w}{m}$$
- $$0 = \frac{-C_L 2k \left( \frac{\rho}{2} \right) V^2 S}{m} [(\lambda_u \cos \gamma_a \cos \chi_a) + (\lambda_v \cos \gamma_a \sin \chi_a) - (\lambda_w \sin \gamma_a)]$$

$$+ \frac{\left( \frac{\rho}{2} \right) V^2 S}{m} \left[ \begin{aligned} &(-\lambda_u \cos \mu_a \sin \gamma_a \cos \chi_a) - (\lambda_u \sin \mu_a \sin \chi_a) - \\ &(\lambda_v \cos \mu_a \sin \gamma_a \sin \chi_a) + (\lambda_v \sin \mu_a \cos \chi_a) - (\lambda_w \cos \mu_a \cos \gamma_a) \end{aligned} \right]$$
- $$\frac{C_L 2k \left( \frac{\rho}{2} \right) V^2 S}{m} \left[ \begin{aligned} &(\lambda_u \cos \gamma_a \cos \chi_a) \\ &+ (\lambda_v \cos \gamma_a \sin \chi_a) \\ &- (\lambda_w \sin \gamma_a) \end{aligned} \right] = - \frac{\left( \frac{\rho}{2} \right) V^2 S}{m} \left[ \begin{aligned} &\lambda_u (\cos \mu_a \sin \gamma_a \cos \chi_a + \sin \mu_a \sin \chi_a) \\ &+ \lambda_v (\cos \mu_a \sin \gamma_a \sin \chi_a - \sin \mu_a \cos \chi_a) \\ &+ \lambda_w \cos \mu_a \cos \gamma_a \end{aligned} \right]$$

### Penurunan persamaan $\mu(t)$

Berdasarkan persamaan (3.4) dan persamaan (3.6) maka dilakukan penurunan-penurunan persamaan untuk mencari persamaan  $\mu(t)$  seperti di bawah ini:

- $$0 = \left( \frac{-\cos \chi_a 2kC_L \left(\frac{\rho}{2}\right) V^2 S - \sin \mu_a \sin \chi_a \left(\frac{\rho}{2}\right) V^2 S}{m} \right) \lambda_u$$

$$+ \left( \frac{-\sin \chi_a 2kC_L \left(\frac{\rho}{2}\right) V^2 S + \sin \mu_a \cos \chi_a \left(\frac{\rho}{2}\right) V^2 S}{m} \right) \lambda_v$$

$$+ \left( \frac{-\cos \mu_a \left(\frac{\rho}{2}\right) V^2 S}{m} \right) \lambda_w$$
- $$\frac{\cos \mu_a \left(\frac{\rho}{2}\right) V^2 S \lambda_w}{m} = \frac{\left(\frac{\rho}{2}\right) V^2 S}{m} \begin{pmatrix} -\lambda_u \cos \chi_a 2kC_L - \lambda_u \sin \mu_a \sin \chi_a \\ -\lambda_v \sin \chi_a 2kC_L + \lambda_v \sin \mu_a \cos \chi_a \end{pmatrix}$$
- $$\cos \mu_a \lambda_w = -2kC_L [\lambda_u \cos \chi_a + \lambda_v \sin \chi_a] + \sin \mu_a [-\lambda_u \sin \chi_a + \lambda_v \cos \chi_a]$$

$$\lambda_w = \frac{-2kC_L}{\cos \mu_a} [\lambda_u \cos \chi_a + \lambda_v \sin \chi_a] + \frac{\sin \mu_a}{\cos \mu_a} [-\lambda_u \sin \chi_a + \lambda_v \cos \chi_a]$$

$$\lambda_w = \frac{-2kC_L}{\cos \mu_a} [\lambda_u \cos \chi_a + \lambda_v \sin \chi_a] - \lambda_u \tan \mu_a \sin \chi_a + \lambda_v \tan \mu_a \cos \chi_a$$

$$0 = \frac{-2kC_L}{\cos \mu_a} [\lambda_u \cos \chi_a + \lambda_v \sin \chi_a] - \lambda_u \tan \mu_a \sin \chi_a + \lambda_v \tan \mu_a \cos \chi_a - \lambda_w$$

### Penurunan persamaan sudut belok optimal ( $(\mu_a)_{opt}$ ) dengan kendala

Persamaan Hamiltonian pada persamaan (3.24) diturunkan terhadap  $\mu_a$  untuk mencari sudut belok optimal ( $(\mu_a)_{opt}$ ) dengan kendala dan berdasarkan persamaan (3.2) didapatkan penurunan-penurunan sebagai berikut:

$$\begin{aligned}
 & 0 = \left\{ -2 \sec^2 \mu_a \tan \mu_a \left( \frac{\cos \gamma_a \cos \chi_a \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \right) - \sec^2 \mu_a \sin \chi_a \cdot g \right\} \lambda_u \\
 & \bullet \quad + \left\{ -2 \sec^2 \mu_a \tan \mu_a \left( \frac{\cos \gamma_a \sin \chi_a \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \right) + \sec^2 \mu_a \cos \chi_a \cdot g \right\} \lambda_v \\
 & \quad + \left\{ 2 \sec^2 \mu_a \tan \mu_a \left( \frac{\sin \gamma_a \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \right) \right\} \lambda_w \\
 & \bullet \quad 0 = \frac{2 \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \left[ -\sec^2 \mu_a \tan \mu_a \cos \gamma_a \cos \chi_a \lambda_u - \sec^2 \mu_a \tan \mu_a \cos \gamma_a \sin \chi_a \lambda_v \right. \\
 & \quad \left. + \sec^2 \mu_a \tan \mu_a \sin \gamma_a \lambda_w \right. \\
 & \quad \left. - \sec^2 \mu_a \sin \chi_a \cdot g \lambda_u + \sec^2 \mu_a \cos \chi_a \cdot g \lambda_v \right] \\
 & \bullet \quad \sec^2 \mu_a \sin \chi_a \cdot g \lambda_u - \sec^2 \mu_a \cos \chi_a \cdot g \lambda_v = \frac{2 \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \left[ -\sec^2 \mu_a \tan \mu_a \cos \gamma_a \cos \chi_a \lambda_u \right. \\
 & \quad \left. - \sec^2 \mu_a \tan \mu_a \cos \gamma_a \sin \chi_a \lambda_v \right. \\
 & \quad \left. + \sec^2 \mu_a \tan \mu_a \sin \gamma_a \lambda_w \right] \\
 & \bullet \quad \lambda_u \sin \chi_a - \lambda_v \cos \chi_a = \frac{-2 \text{ kmg}^2}{\left(\frac{\rho}{2}\right) V^2 S} \tan \mu_a \left[ \lambda_u \cos \gamma_a \cos \chi_a + \lambda_v \cos \gamma_a \sin \chi_a \right. \\
 & \quad \left. - \lambda_w \sin \gamma_a \right]
 \end{aligned}$$

**LAMPIRAN C**  
**BLOK SIMULINK**

